

Code No: 156AZ

JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD

B. Tech III Year II Semester Examinations, March - 2024

FINITE ELEMENT METHODS

(Common to ME, MCT)

Time: 3 Hours

Max. Marks: 75

- Note:** i) Question paper consists of Part A, Part B.  
 ii) Part A is compulsory, which carries 25 marks. In Part A, Answer all questions.  
 iii) In Part B, Answer any one question from each unit. Each question carries 10 marks and may have a, b as sub questions.

**PART – A****(25 Marks)**

- 1.a) What are the basic approaches to improving a finite element model? [2]  
 b) Write the advantages and applications of FEM. [3]  
 c) Write the equation for transforming the local stiffness equation into the global stiffness equation. [2]  
 d) Write down the essential and natural boundary conditions of the problem (figure 1). [3]

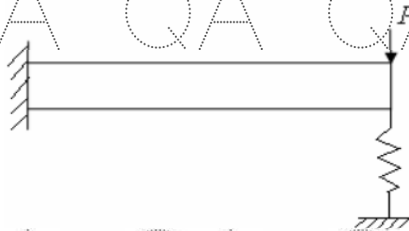


Figure 1

- e) Differentiate among the Iso-parametric and Sub-parametric formulations. [2]  
 f) How axisymmetric elements can be equalized to the CST element? [3]  
 g) What do you mean by steady state heat transfer analysis? [2]  
 h) Define heat transfer? Write the finite element equation for 1-D heat conduction with free end convection? [3]  
 i) Explain mesh generation techniques in FEM. [2]  
 j) Discuss the NASTRAN software used to evaluate the problems in FEM hexahedral and tetrahedral elements. [3]

**PART – B****(50 Marks)**

2. Discuss the following methods to solve the given differential equation with the boundary condition  $y(0) = 0$  and  $y(x) = 0$ , (a) Subdomain method (b) Weighted residual method. [10]

$$EI \frac{d^2 y}{dx^2} M(x) = 0$$

**OR**

- 3.a) Explain the potential energy formulation for obtaining element equations in Finite element methods.  
 b) With a suitable example, explain any weighted residual method. [5+5]

4. For the two-bar truss shown in the figure 2, determine the displacements and stress.  $A_1=500\text{mm}^2$ ,  $A_2=1200\text{mm}^2$ ,  $E=2 \times 10^5 \text{ N/mm}^2$ . [10]

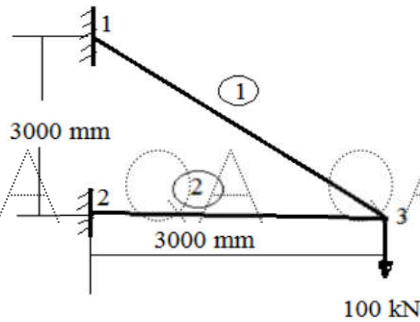


Figure 2  
OR

- 5.a) Mention an expression for stiffness matrix for 2D-truss element.  
b) For the beam and loading shown in figure 3, Determine; (i) slope at 2 and 3 (ii) vertical deflection at the midpoint of the load Take  $E=200\text{GPa}$ ,  $I= 4 \times 10^6 \text{ mm}^4$ . [2+8]

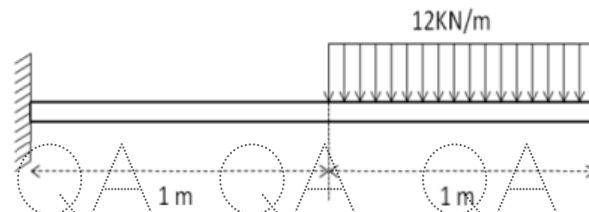


Figure 3

6. Determine the stiffness matrix for the axisymmetric element shown in the figure 4. Take  $E = 2.1 \times 10^6 \text{ N/mm}^2$  and Poisson's ratio as 0.3. All dimensions are in mm only. [10]

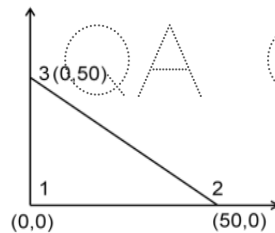


Figure 4  
OR

- 7.a) Derive the stiffness matrix for the four-noded quadrilateral element in terms of natural coordinate system.  
b) Differentiate between CST and LST with respect to the triangular element. [6+4]

8. For the composite wall shown in the figure 5 determine the interface temperatures considering three elements. [10]

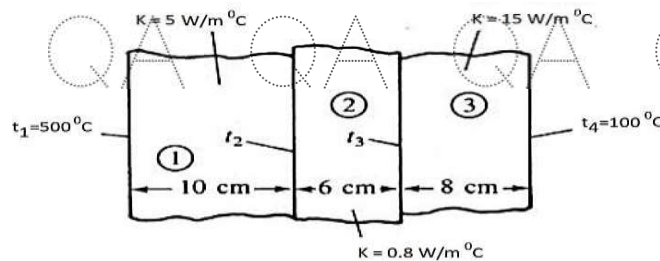


Figure 5

QA

9.

Determine the temperature distribution in a 1D rectangular cross section fin with 8cm long, 4cm wide, 1cm thick. Assume that convective heat loss occurs from the end of the fin. Take  $K = 3W/cm K$ ,  $h = 0.1W/cm^2k$  and  $T_a = 200^\circ C$ . Tip temperature is  $1000^\circ C$ .

[10]

OR

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10.

Determine the Eigen values and Eigen vectors of the bar shown in figure 6. Take  $E=200 Gpa$ ,  $\rho = 7862 kg/m^2$ ,  $A=6 cm^2$  and  $L=2.5 m$ .

[10]

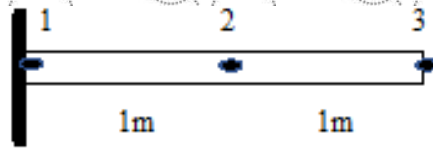


Figure 6

QA

11.

Discuss Eigen value and Eigen vector analysis of stepped bar and truss.

[10]

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